COL749: Computational Social Choice

Lecture 6 (Contd.)
Kidney Exchange

Housing Market

[Shapley and Scarf, JME 1974]

Housing Market

[Shapley and Scarf, JME 1974]





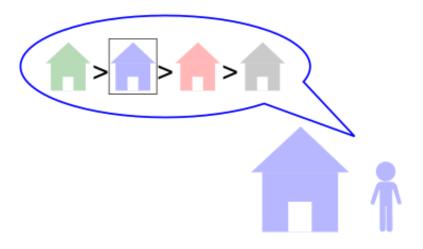


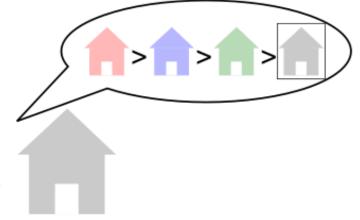


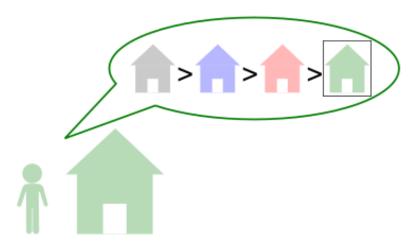
Housing Market

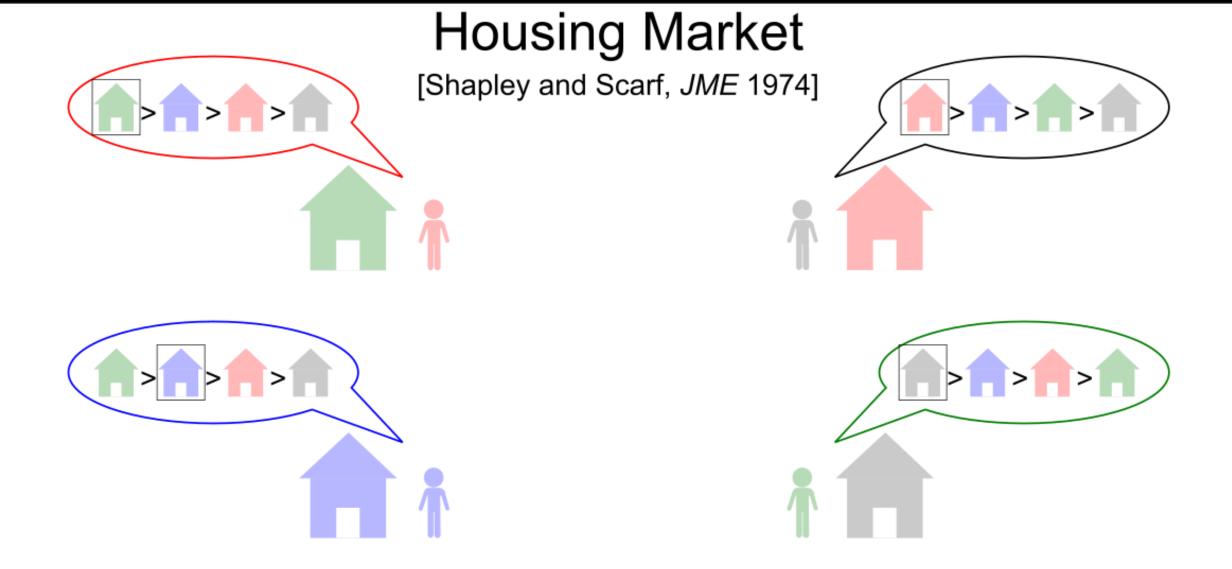












Is there a way to exchange houses to make the agents "maximally happy"?

Top-Trading Cycle Algorithm (TTCA)

[Shapley and Scarf, JME 1974 (attributed to David Gale)]

While there is a remaining agent:

- Each remaining agent points to the owner of its favorite house.
- There must be a cycle (include self-loops). Do the cyclic exchange.
- Remove the agents and houses involved in the above exchange.

The Core

An allocation is in the core if no coalition blocks it.

A coalition of agents blocks an allocation A if:

they can redistribute their **endowed houses** among themselves such that, compared to A, none of them is worse off and at least one of them is strictly better off (i.e., redistributing endowments is a Pareto improvement over A).

Awesome Properties of TTCA

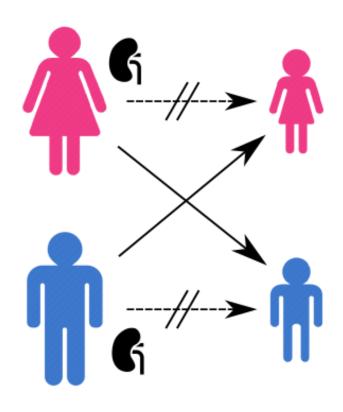
Polynomial running time

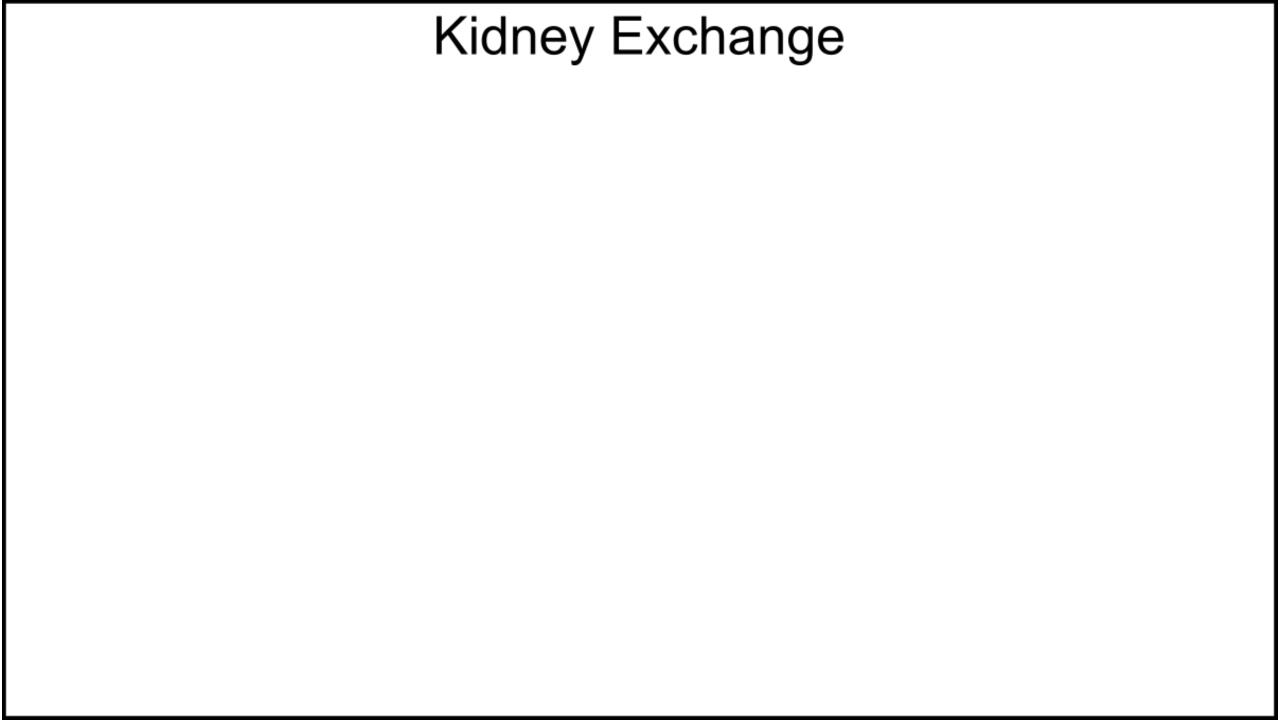
(Group) strategyproof

Core

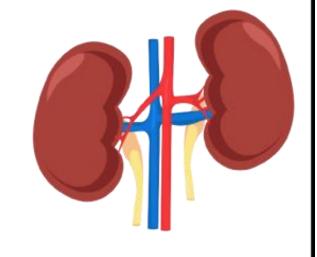
Pareto optimal

Application of TTCA

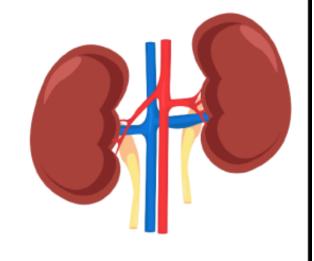


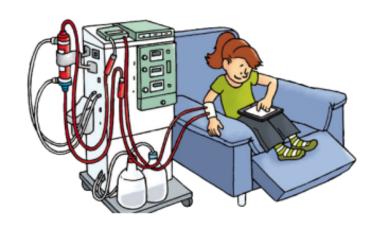


Many people suffer from kidney failure (waiting list in US: ~90,000; in India: ~200,000).



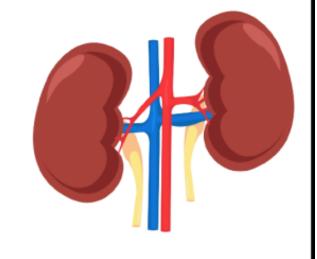
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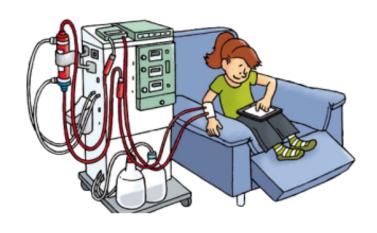




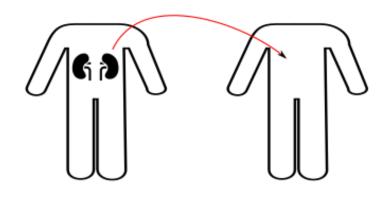
Dialysis

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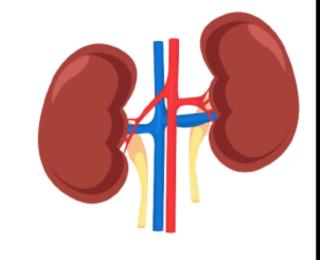


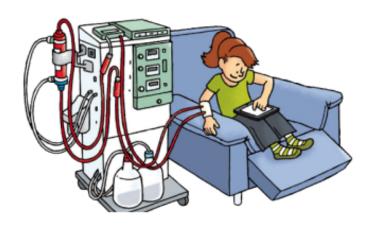


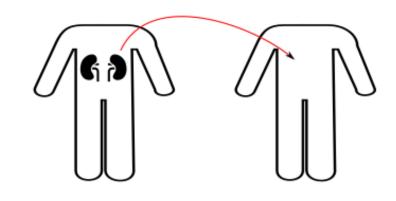


Transplant

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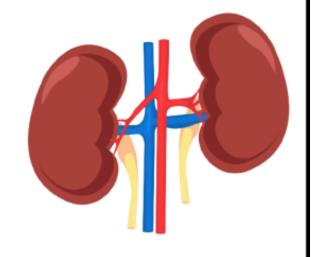


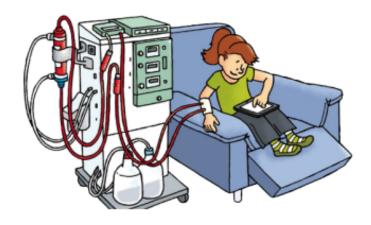
Dialysis

Poor quality of life High cost **Transplant**

Better life quality Lower cost

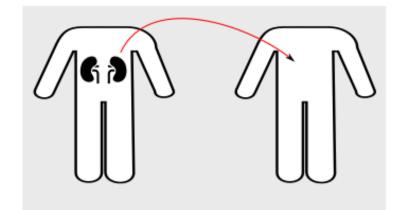
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Dialysis

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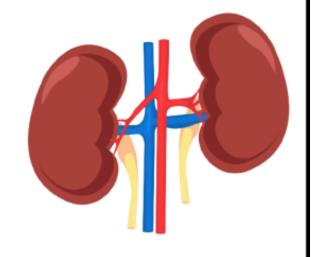


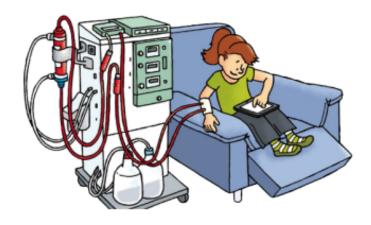
Transplant

Better life quality Lower cost From a deceased donor

From a living donor

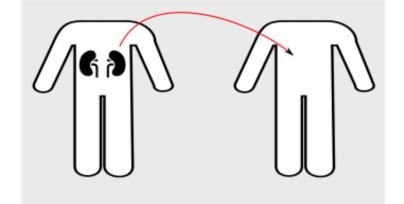
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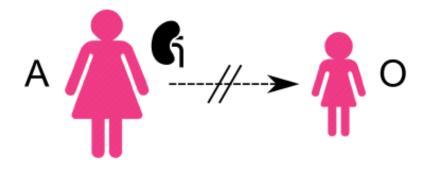
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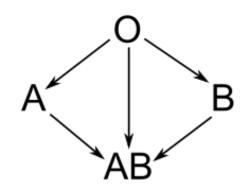
E.g., first-degree relatives, spouse etc.

Simply having a willing donor is not enough. The organ must be medically compatible.

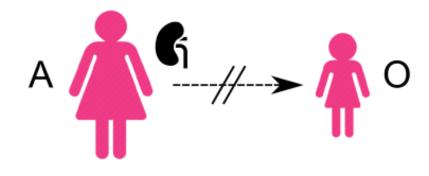
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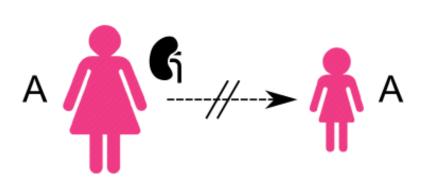
Blood-type incompatibility



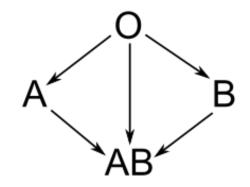


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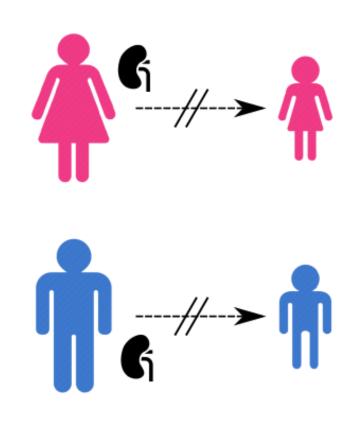
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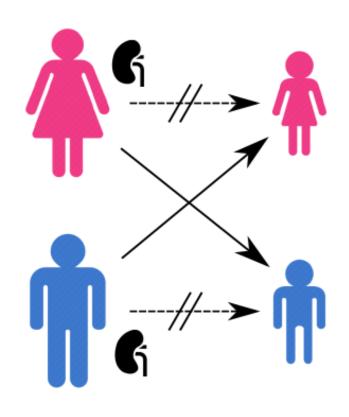
Tissue-type incompatibility

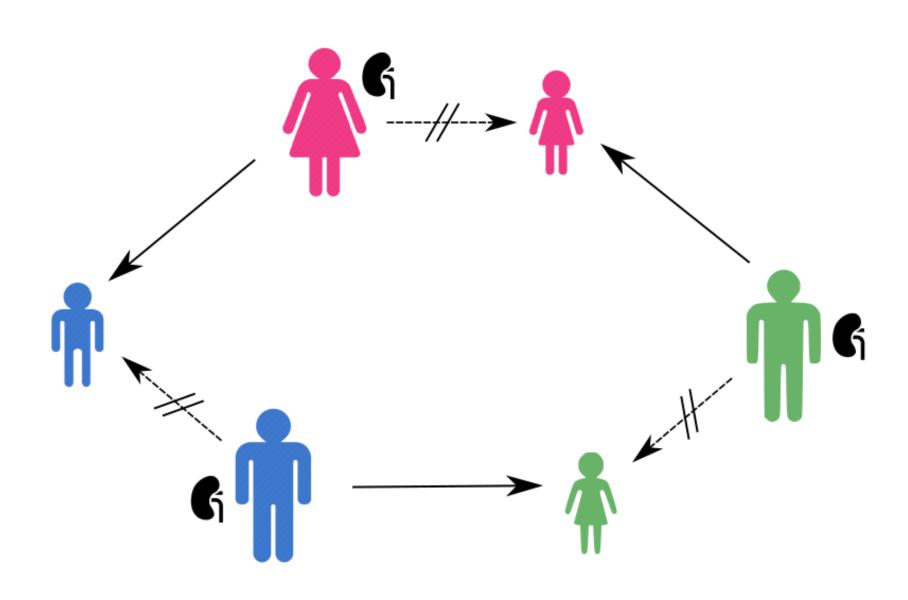
Sensitized patients with antibodies that will attack a foreign tissue (often due to prior exposure during blood transfusion, pregnancy, previous transplants).

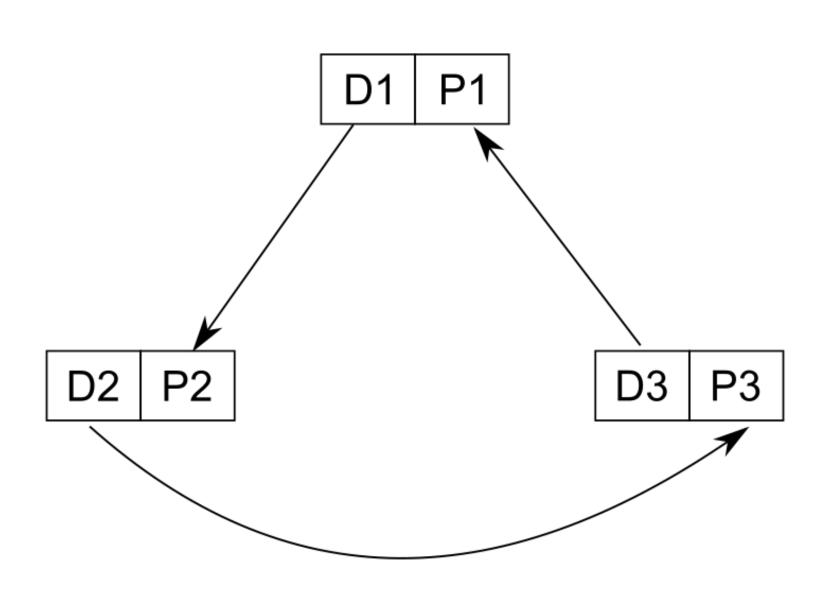
[Rapaport, Transpl. Proc. 1986; Ross et al. NEJM 1997]

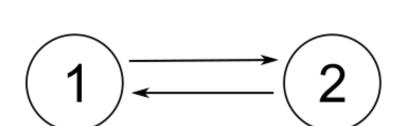


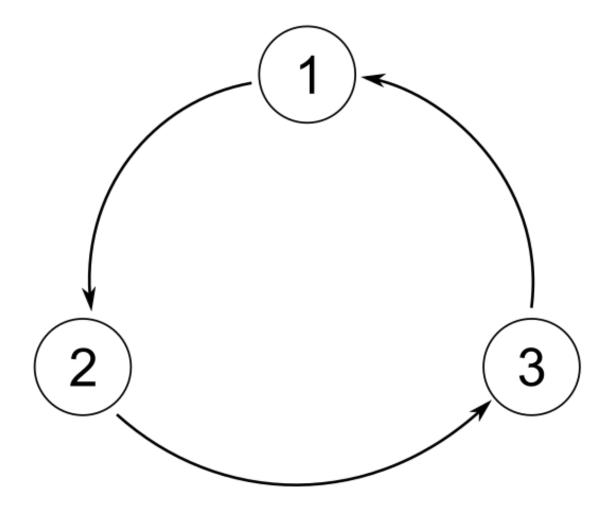
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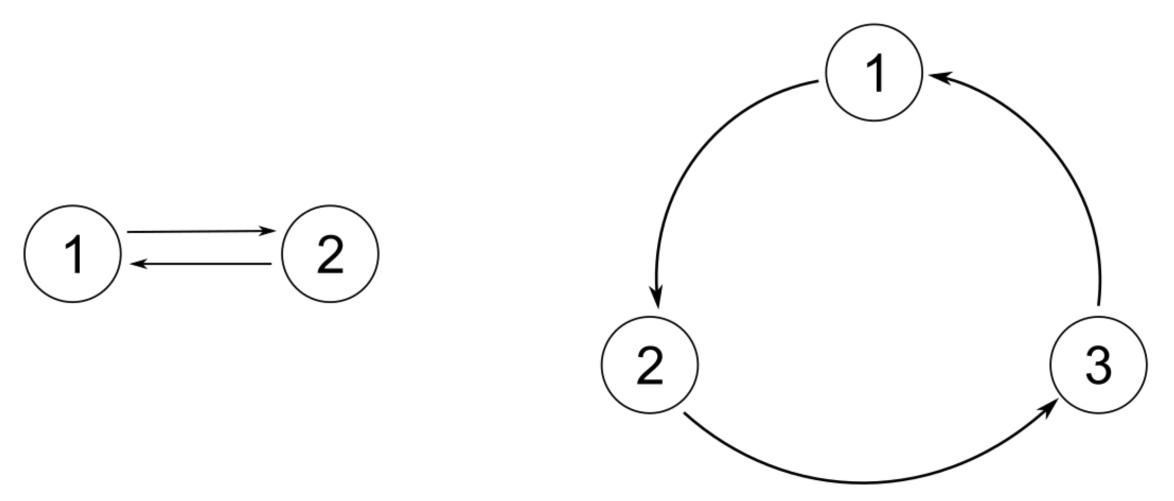












Intuitively, having more and more of such willing-but-incompatible pairs will create more opportunities for an exchange.

History [edit]

Year	Event
1986	KPD first suggested by Rapaport ^[14]
1991	First KPD program started in South Korea by Dr. Park ^[8]
1999	First European KPD transplants performed in Switzerland ^[8]
2000	First KPD transplants performed in USA at the Rhode Island Hospital ^[8]
2001	Hopkins completes KPD transplants and begins first KPD program in USA ^[15]
2004	Dutch established first national KPD program ^[8]
2007	NEAD chain started by APD utilizing first bridge donor ^[16]
2007	Charlie Norwood Living Organ Donation Act clarifies legality of KPD in USA [17]
2008	National Kidney Registry organizes its first transplants on Valentine's Day ^[18]
2009	Hopkins leads first 16 patient multicenter Domino Chain [19][20]
2010	UNOS organizes its first KPD transplants ^[8]
2012	National Kidney Registry completes largest chain involving 60 participants ^[6]
2014	National Kidney Registry sets new record with 70 participant chain ^[7]
2017	First Academic Paper published on "Chronological Incompatibility" outlining the ADP Voucher Program"[21]

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Early Proposals for Kidney Exchange

Proposal 1

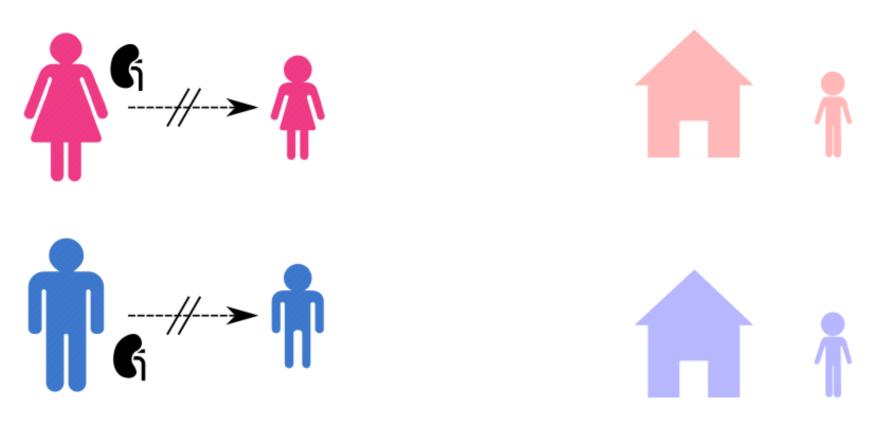
Proposal 2



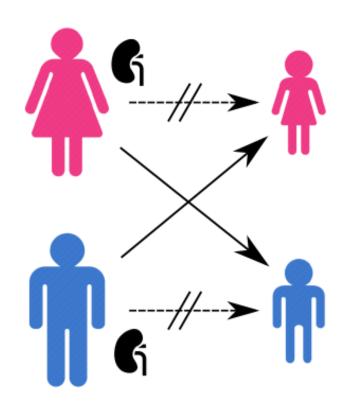


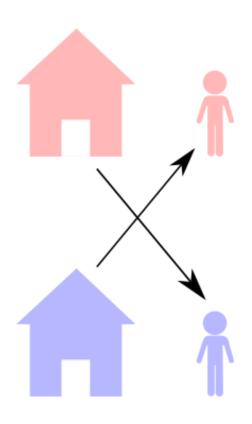
[Roth, Sönmez, and Ünver, QJE 2004]

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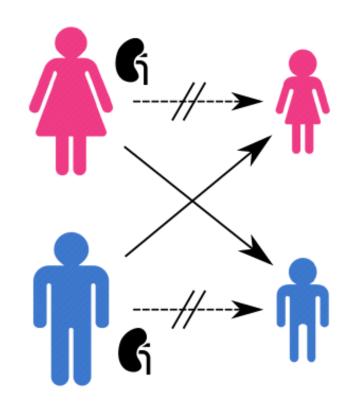


[Roth, Sönmez, and Ünver, QJE 2004]

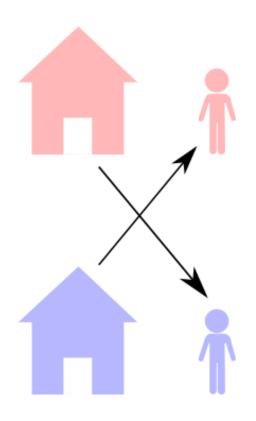




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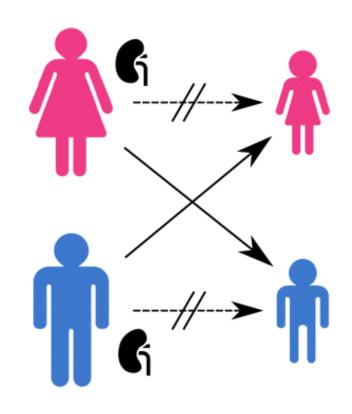


Each patient has a strict ranking of donors.

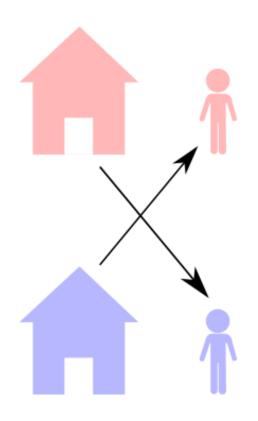


Each agent has a strict ranking of houses.

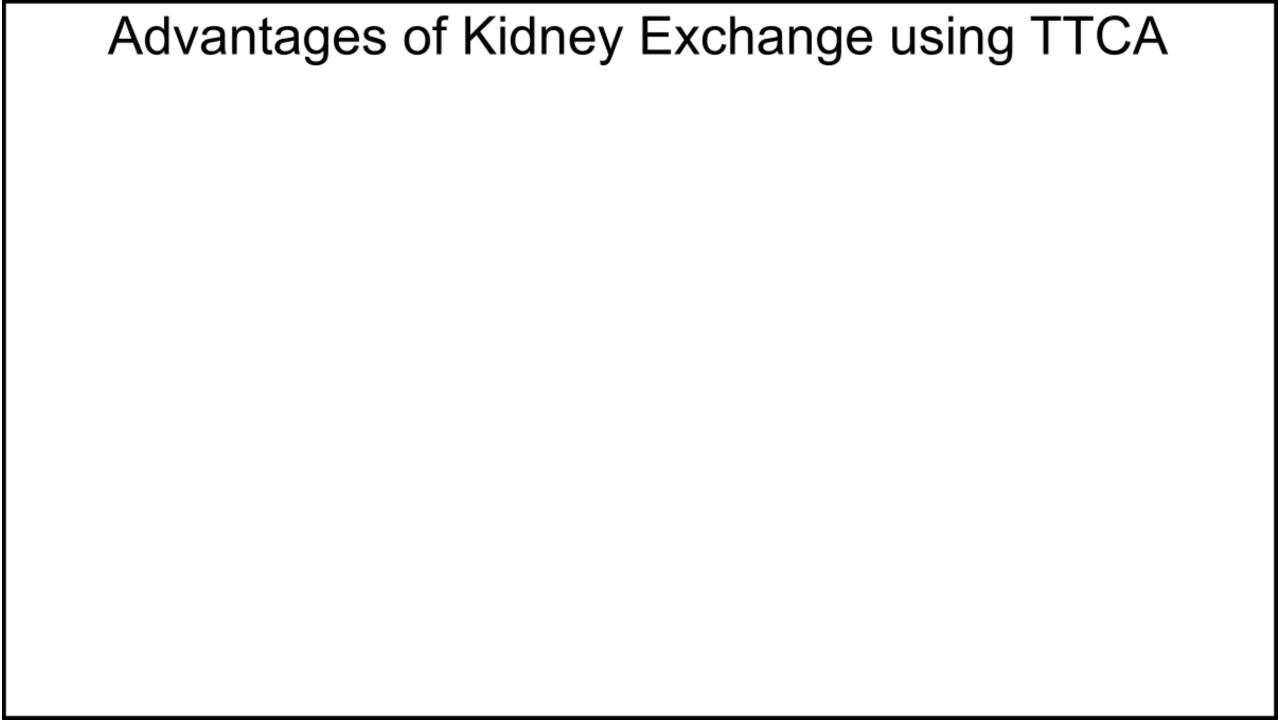
[Roth, Sönmez, and Ünver, QJE 2004]



Each patient has a strict ranking of donors. (medically determined)



Each agent has a strict ranking of houses. (idiosyncratic)



Advantages of Kidney Exchange using TTCA



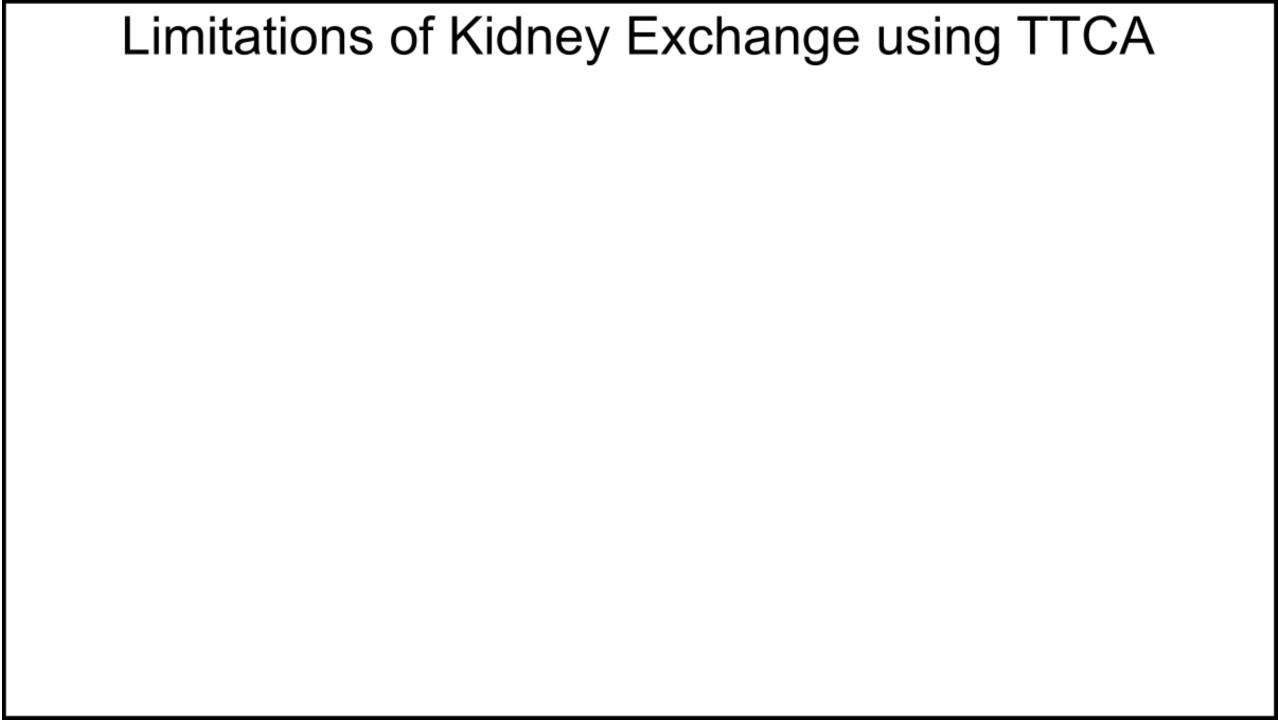
No group of patients can strictly improve by reallocating donors among themselves.



Every patient is (weakly) better off than before.



Polynomial time.





In practice, there may be:

- patients without a donor ("agents without a house")
 - deceased donors ("house without an owner").



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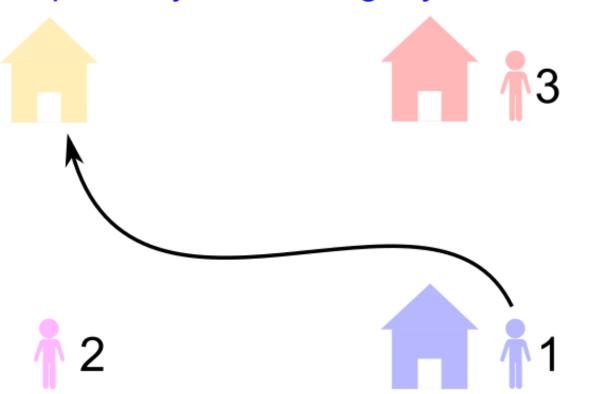








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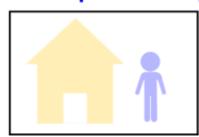






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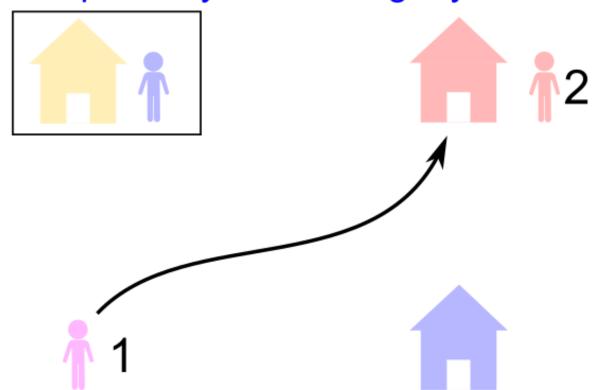








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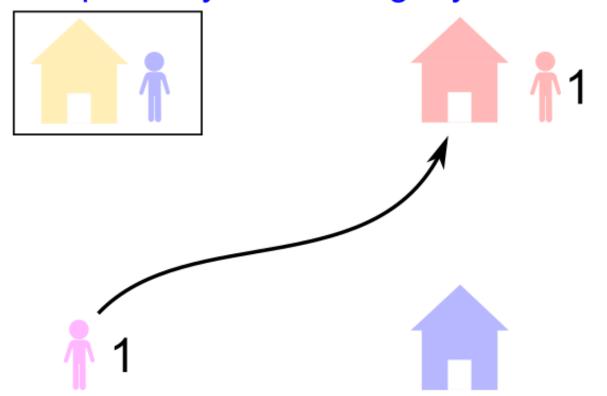






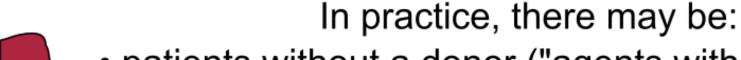


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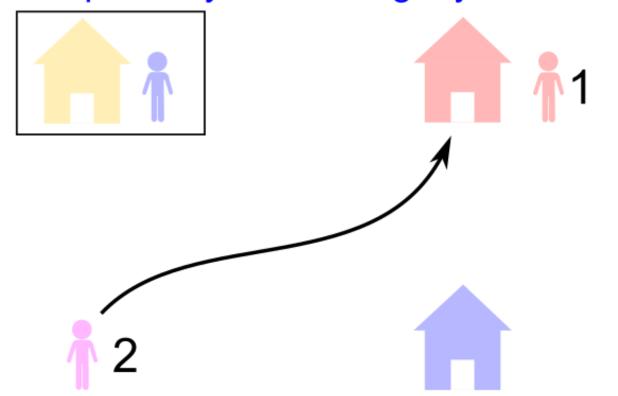








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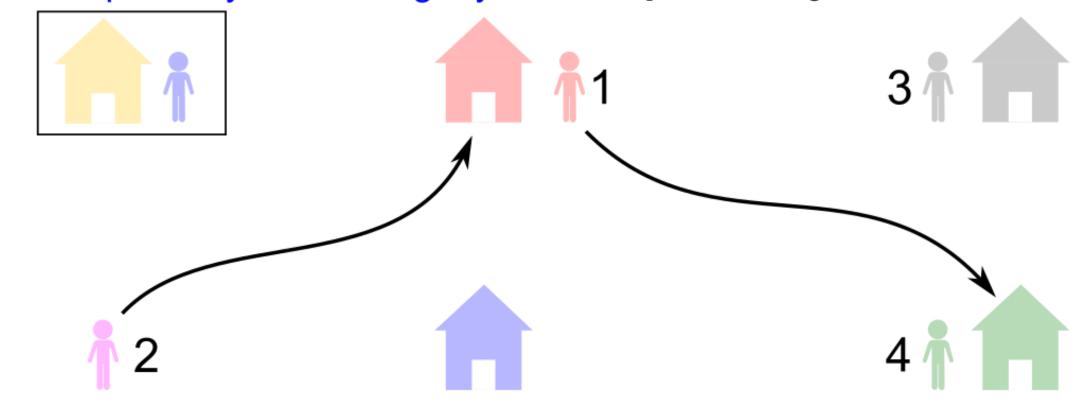






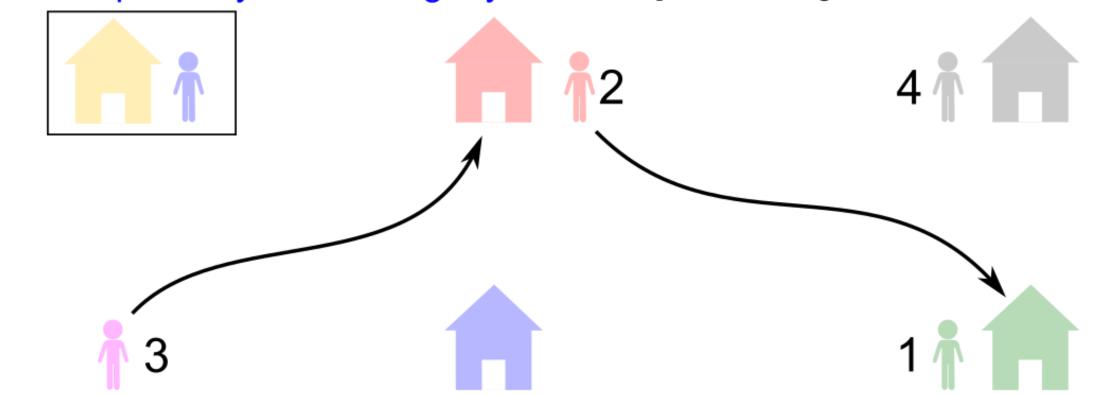


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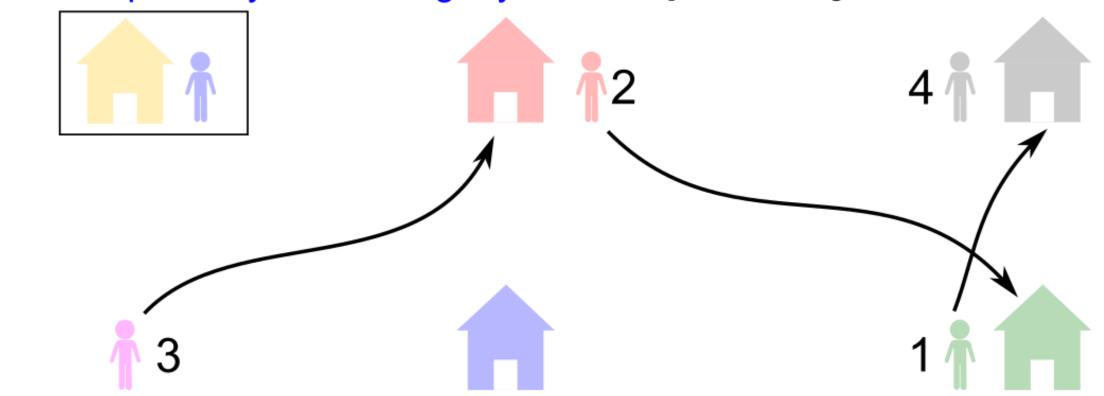


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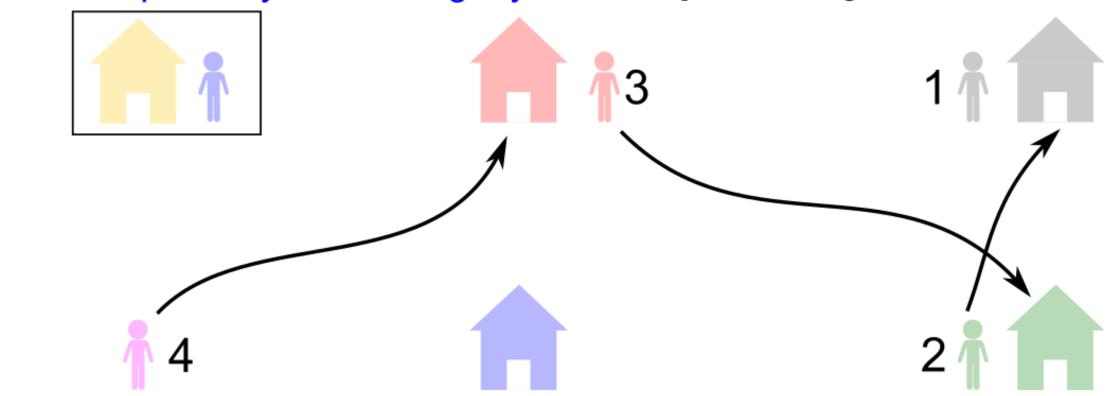


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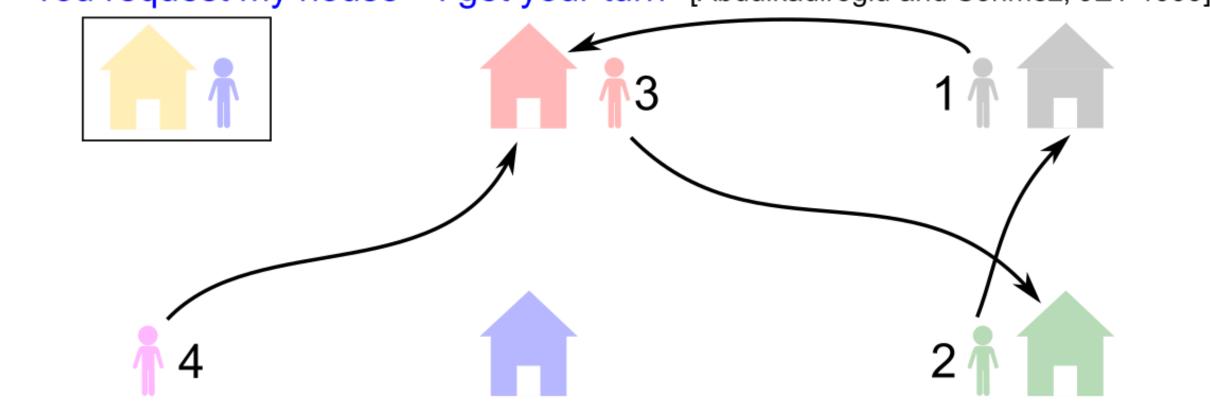


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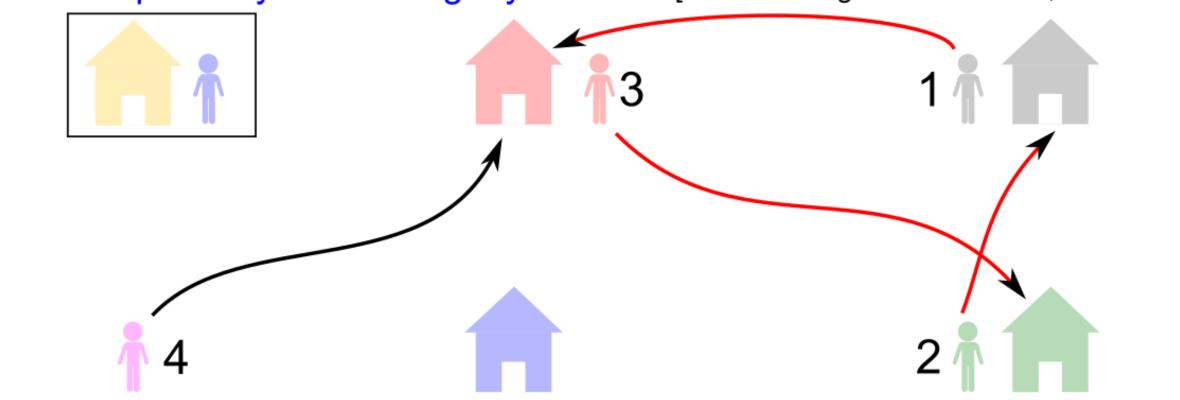


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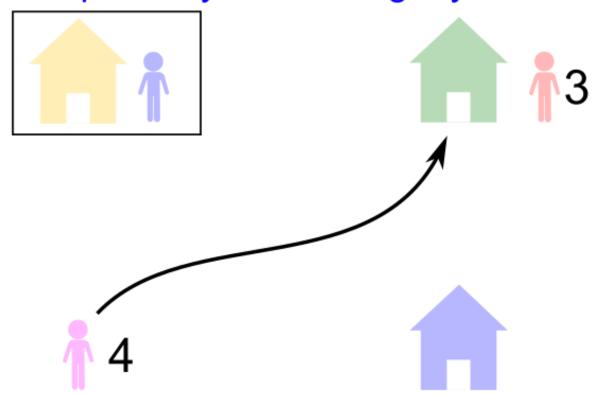


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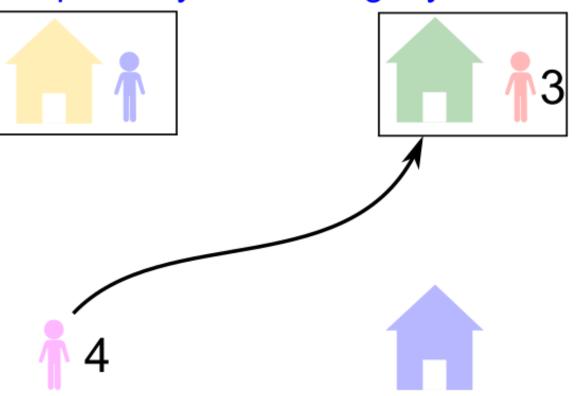








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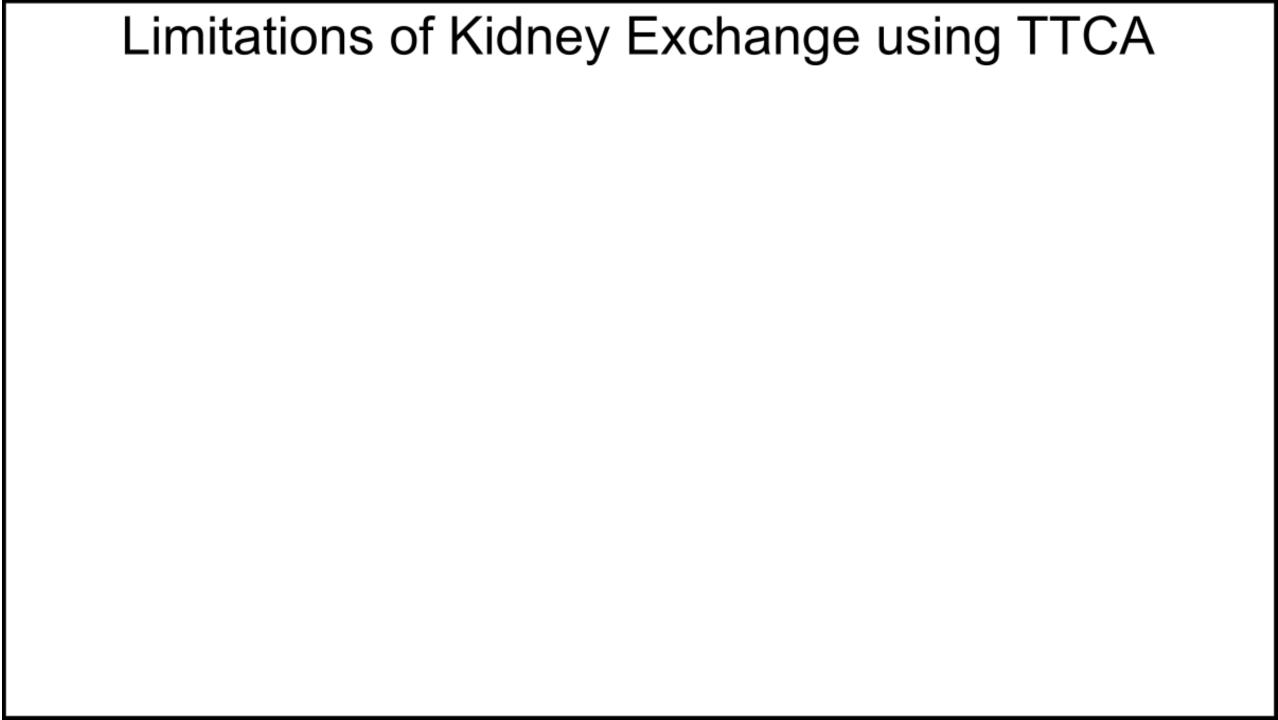






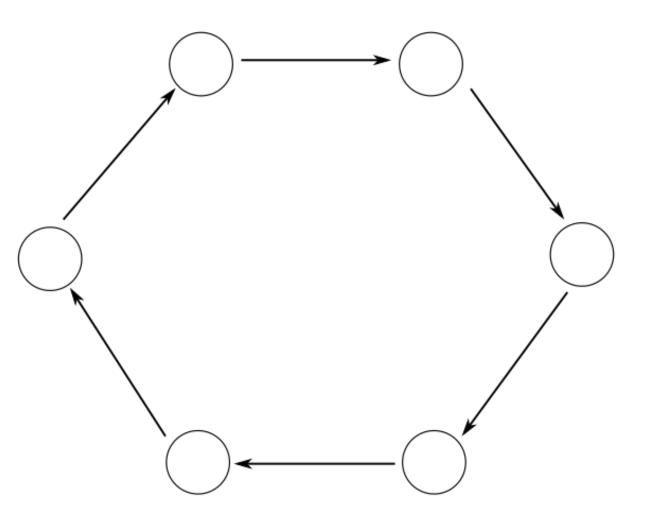


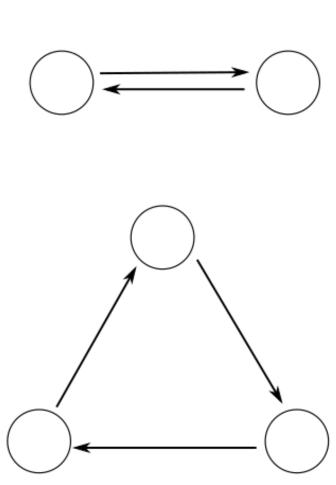




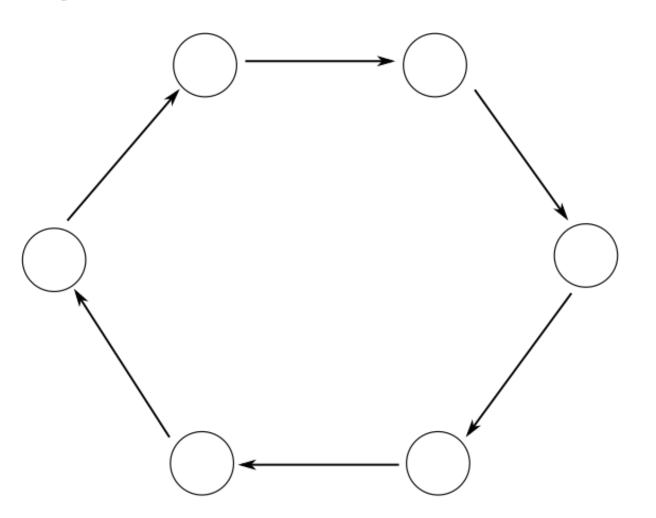


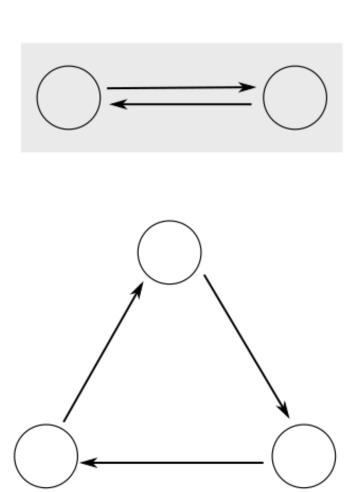




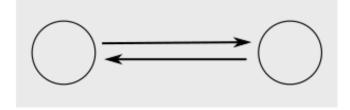




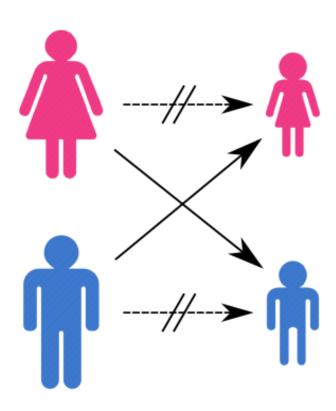








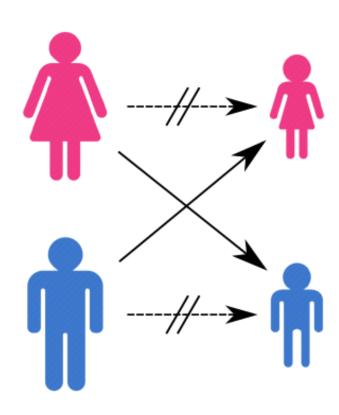


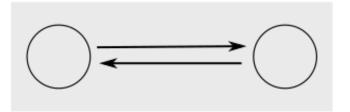






Long cycles can lead to logistical problems.

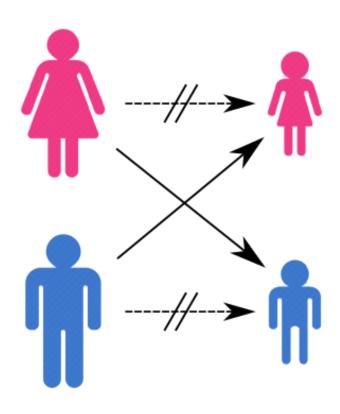


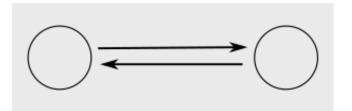


Four surgeries



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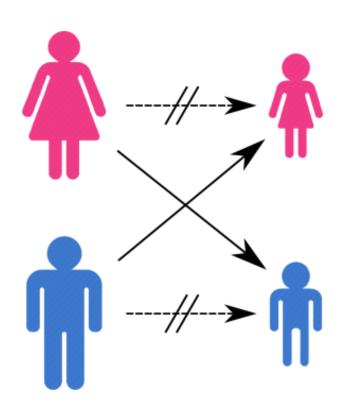


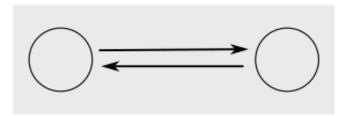


Four simultaneous surgeries



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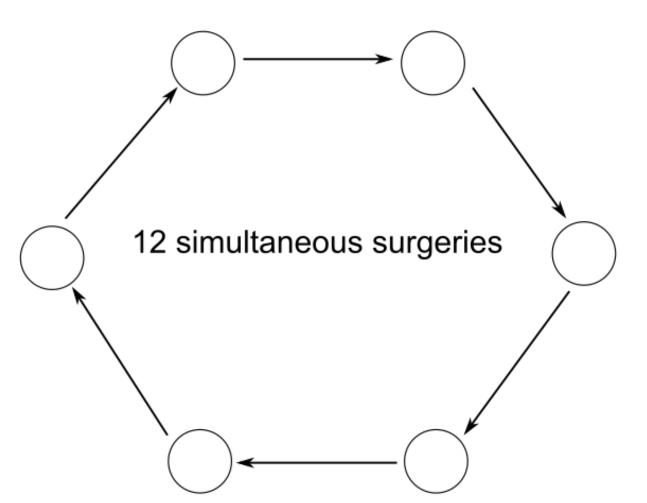
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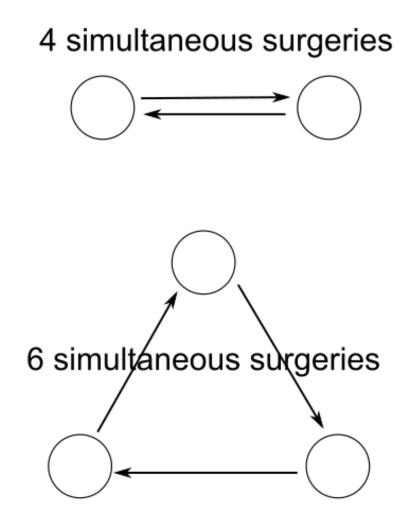
Cannot risk doing

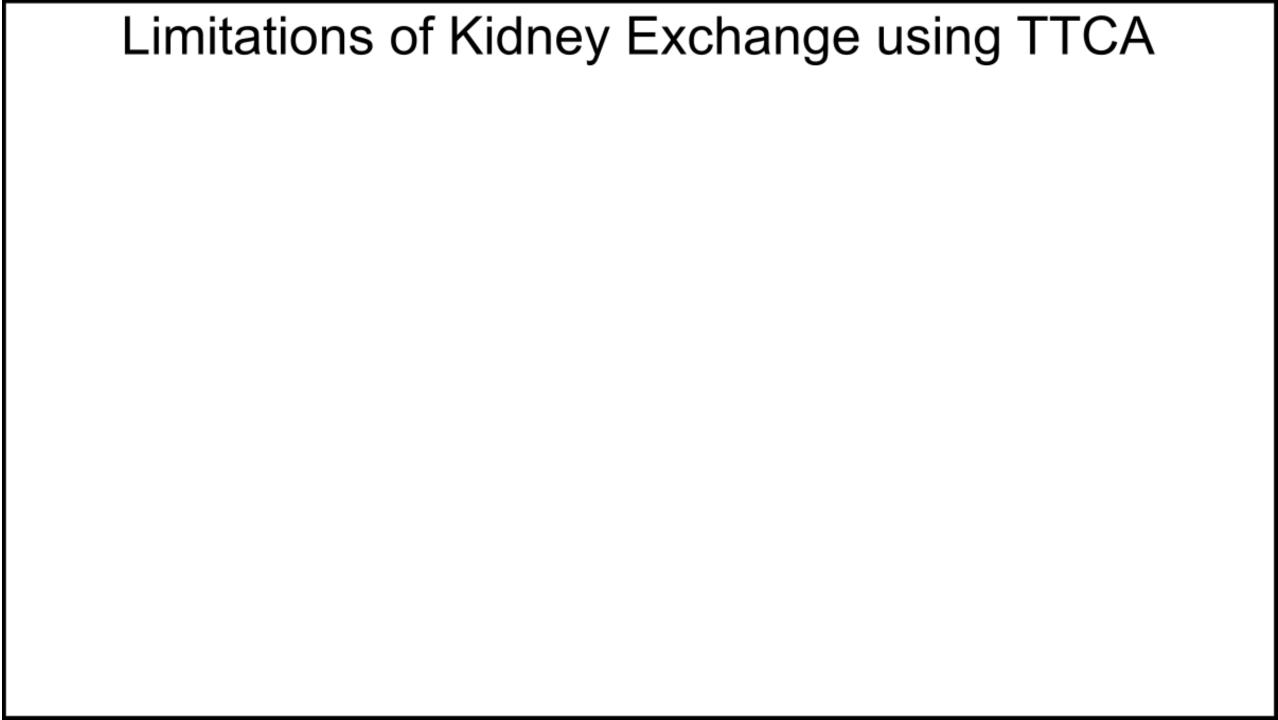












Limitations of Kidney Exchange using TTCA



Strict preferences might be an overkill.

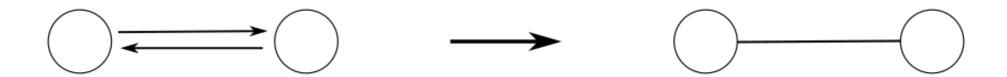
Binary preferences (compatible or incompatible) often suffice.

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Early Proposals for Kidney Exchange

Proposal 1

Using TTCA

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Proposal 2



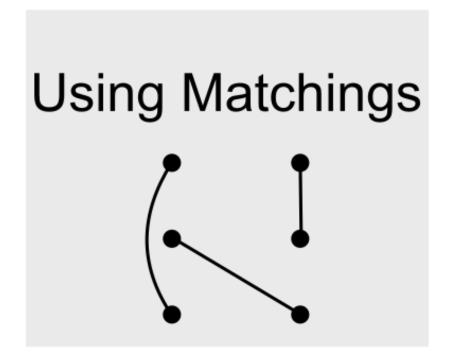
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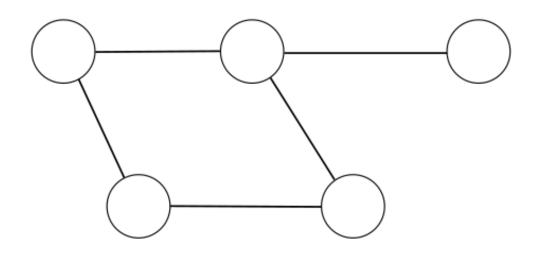
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Proposal 2

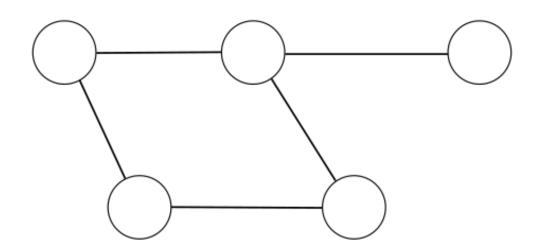


[Roth, Sönmez, and Ünver, JET 2005]

[Roth, Sönmez, and Ünver, JET 2005]

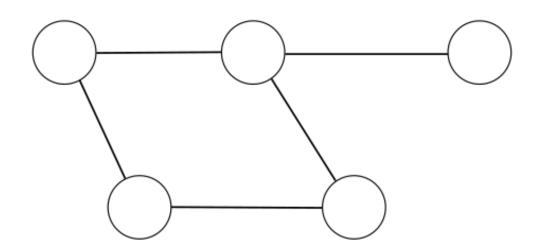


[Roth, Sönmez, and Ünver, JET 2005]



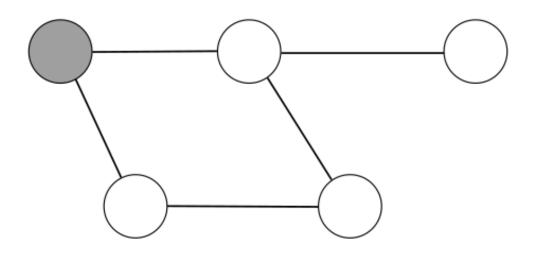
Given an undirected graph (of patient-donor pairs), find a maximum cardinality matching.

[Roth, Sönmez, and Ünver, JET 2005]



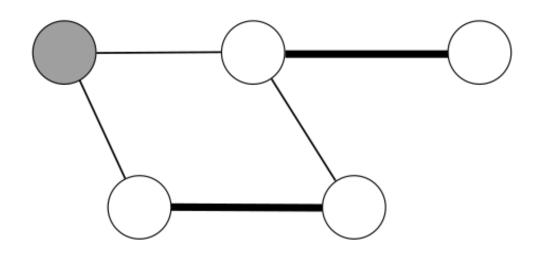
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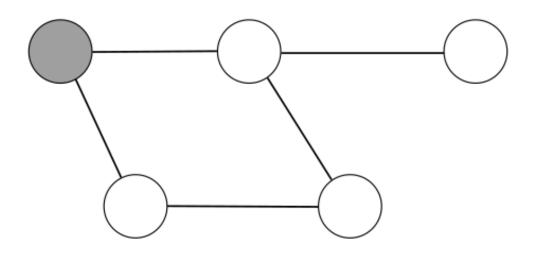
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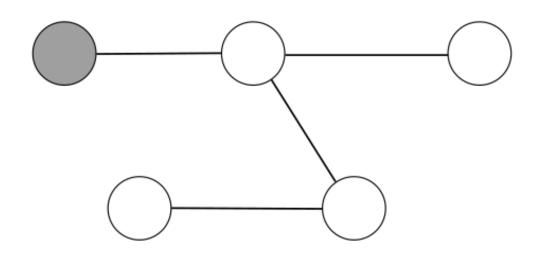
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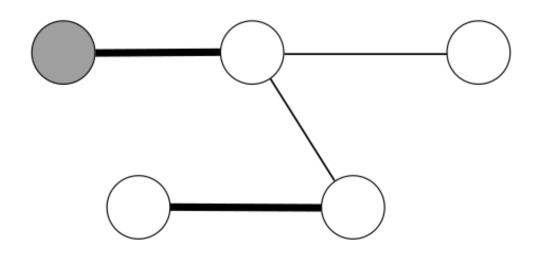
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Priority Mechanism

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Consider a priority ordering 1,2,...,n over vertices (can't be misreported).

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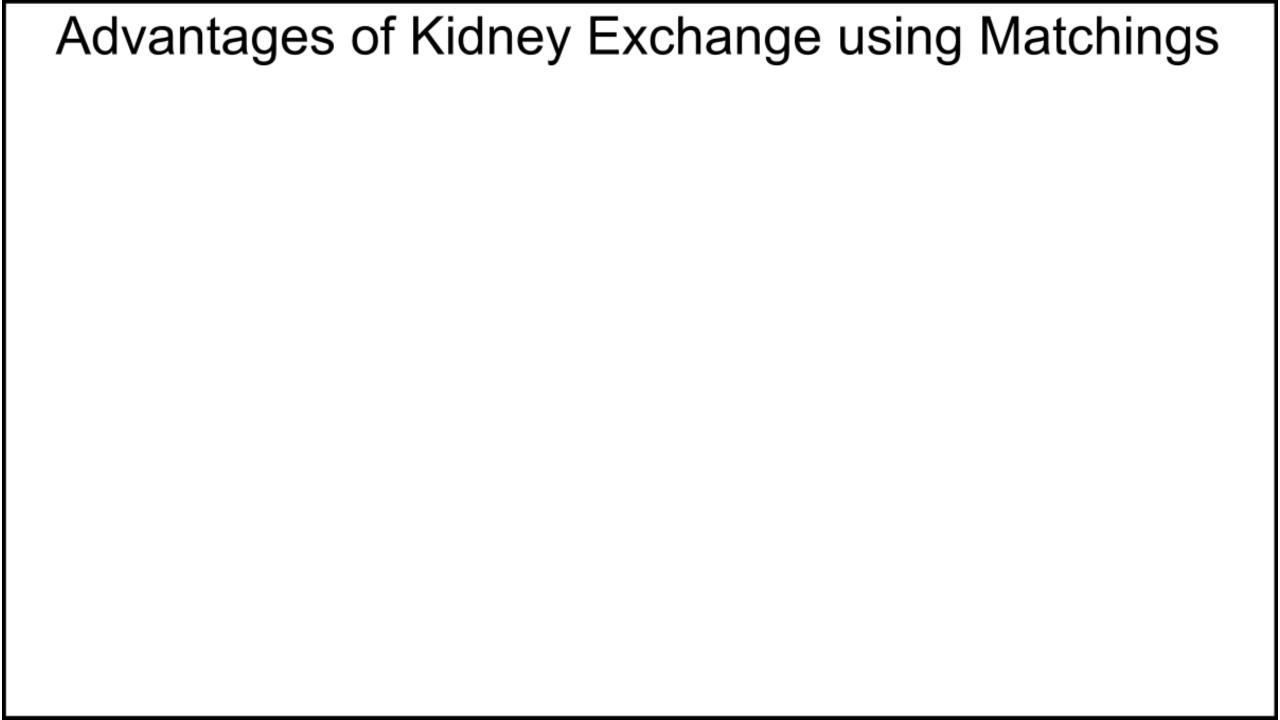
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return M_n





Each matching in M_n matches the same set of vertices.



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No agent will "underreport" the set of its compatible edges.



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The resulting matching is Pareto optimal (no other matching can match a superset of the matched agents).



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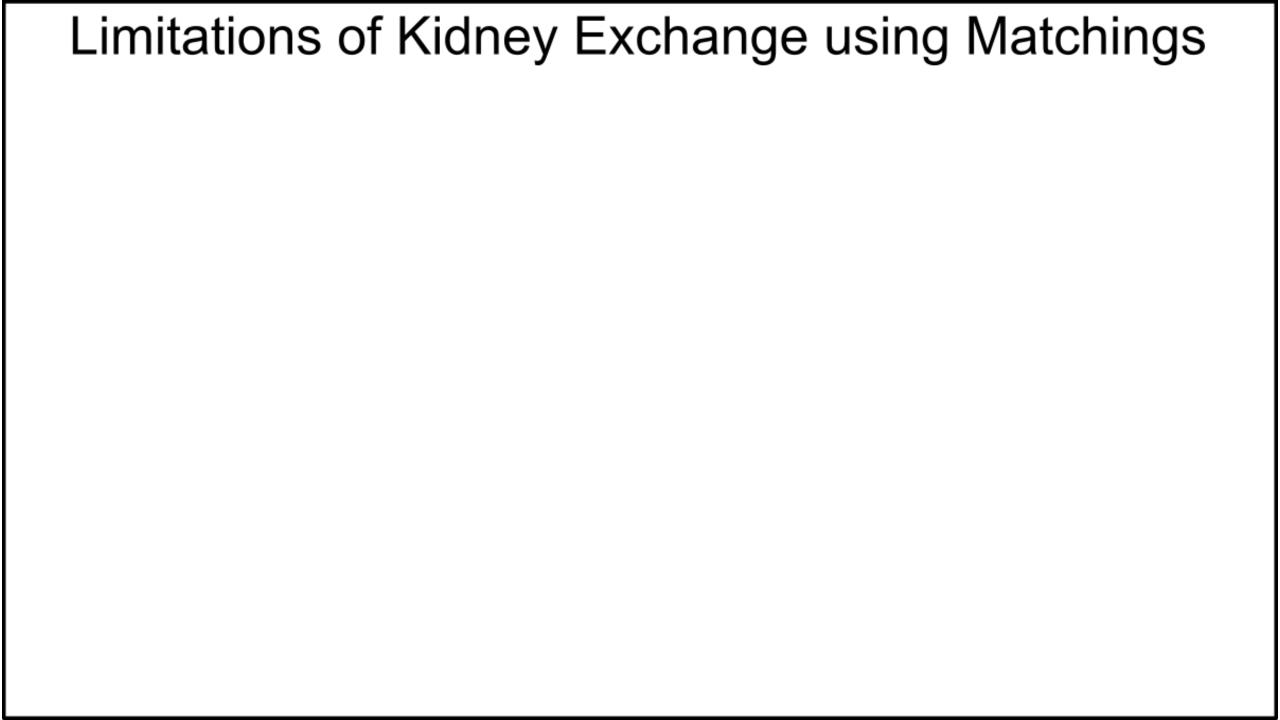


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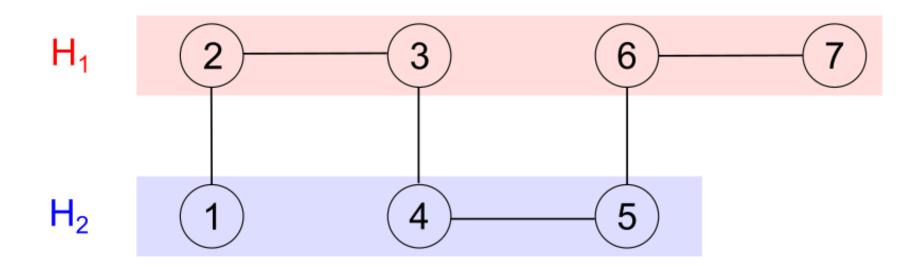
Polynomial time

(uses Edmonds-Gallai decomposition from Graph Theory)

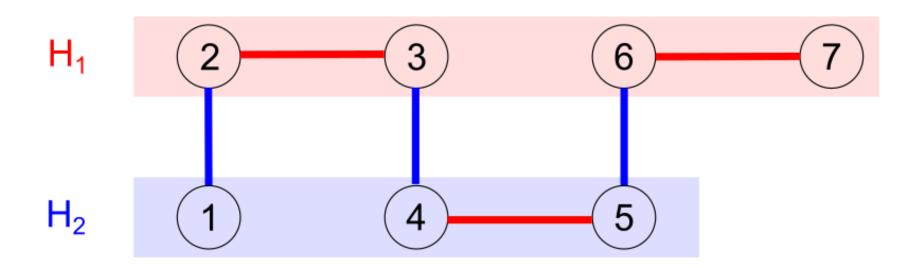




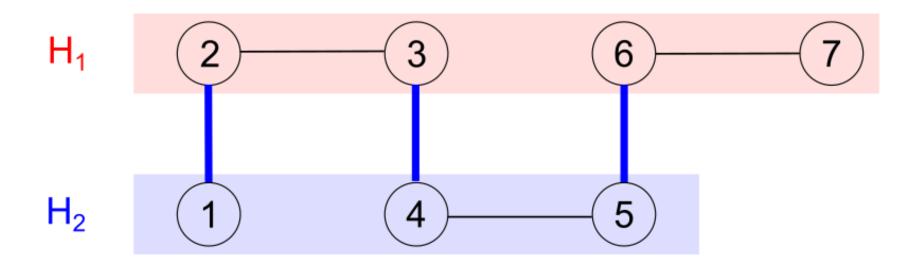






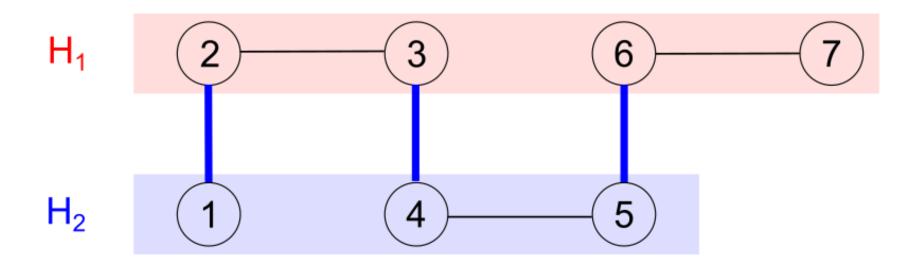








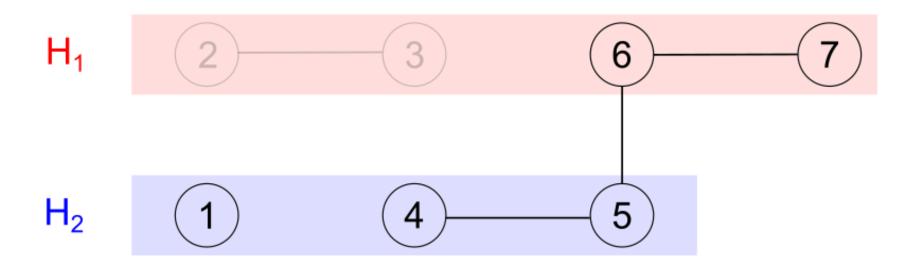
As kidney exchange has evolved, the game has shifted. It is the hospitals, and not the individual patient-donor pairs, that have become the new "players".



Hospital H₁ can match (2) and (3) internally (i.e., not disclose these pairs to the matching algorithm) and have all of its patients matched.



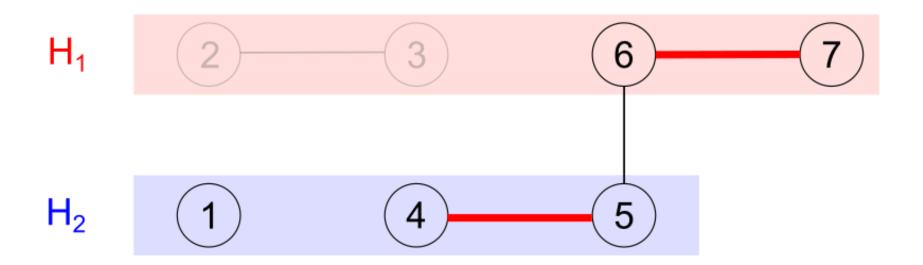
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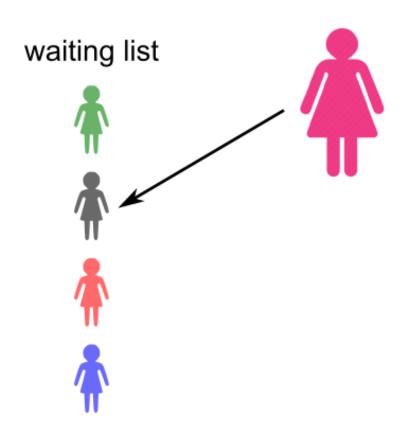
History [edit]

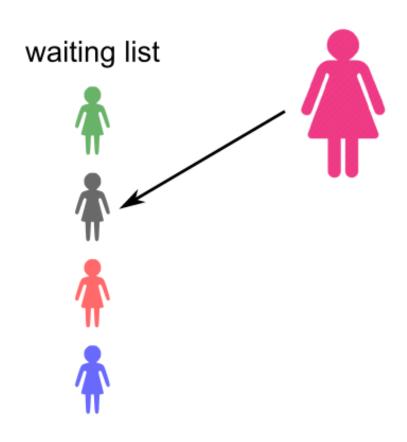
Year	Event
1986	KPD first suggested by Rapaport ^[14]
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1999	First European KPD transplants performed in Switzerland ^[8]
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2001	Hopkins completes KPD transplants and begins first KPD program in USA ^[15]
2004	Dutch established first national KPD program ^[8]
2007	NEAD chain started by APD utilizing first bridge donor ^[16]
2007	Charlie Norwood Living Organ Donation Act clarifies legality of KPD in USA [17]
2008	National Kidney Registry organizes its first transplants on Valentine's Day ^[18]
2009	Hopkins leads first 16 patient multicenter Domino Chain [19][20]
2010	UNOS organizes its first KPD transplants ^[8]
2012	National Kidney Registry completes largest chain involving 60 participants ^[6]
2014	National Kidney Registry sets new record with 70 participant chain ^[7]
2017	First Academic Paper published on "Chronological Incompatibility" outlining the ADP Voucher Program"[21]

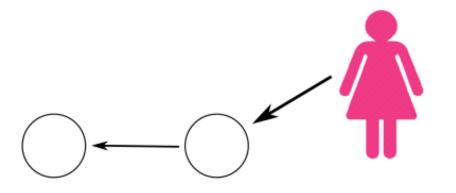
History [edit]

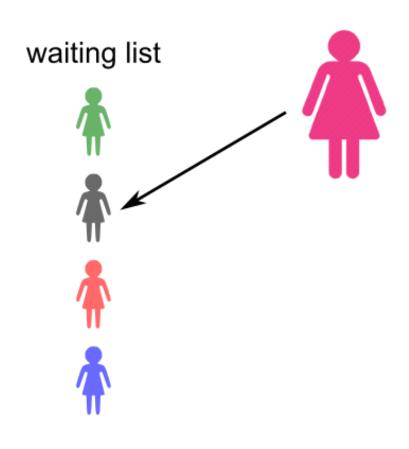
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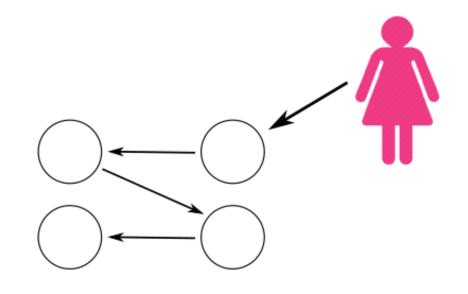


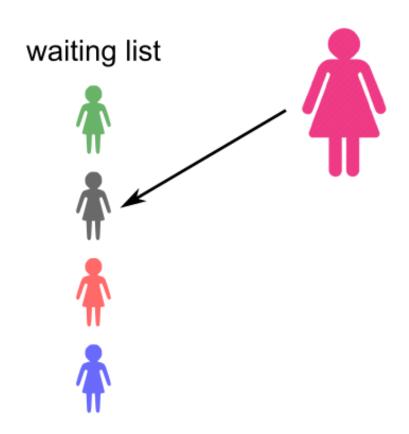


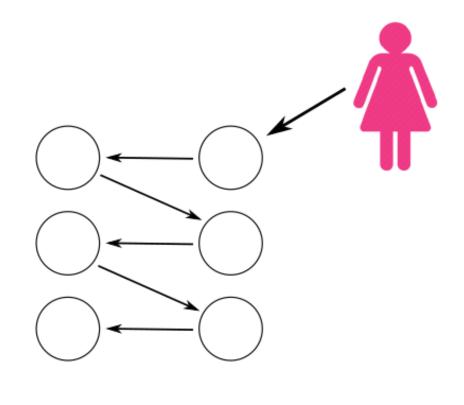


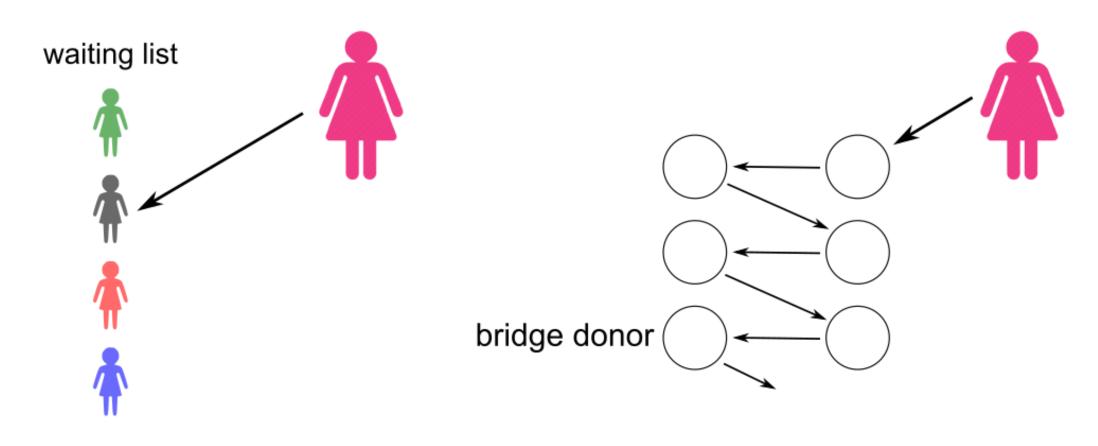




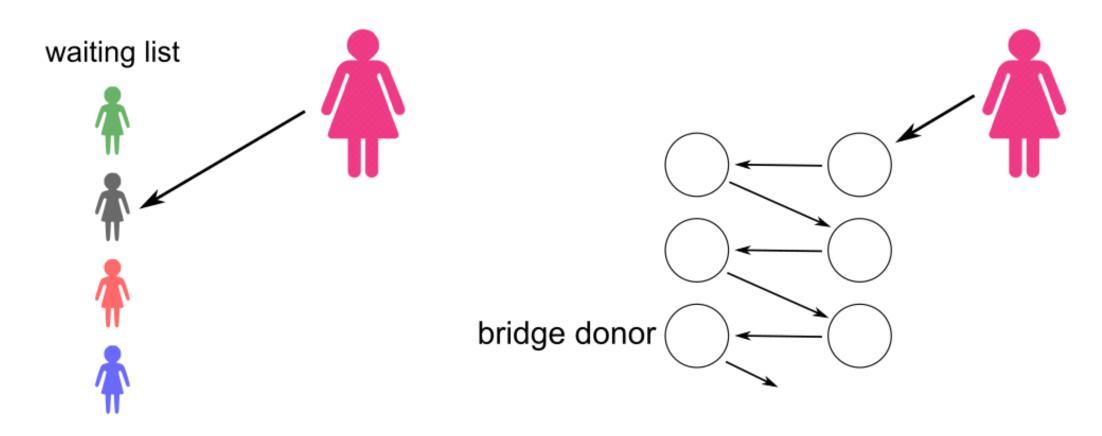








Donors who want to donate an organ without a designated recipient (also known as a *non-directed* or *Good Samaritan* donor)



Transplants in an altruistic donor chain can be done non-simultaneously.

THE KIDNEY CHAIN How a single organ donation changed 20 lives and created the longest-running transplant chain



MATT JONES, 30 Petoskey, Mich. First donor



BARBARA **BUNNELL, 56** Phoenix



BUNNELL, 56 Phoenix



Toledo, Ohio

LAURIE SARVO, 54 Toledo, Ohio



REYNALDO ESPINOZA, 59 Germantown, Md.



CLAUDIA ALAS, 32 Germantown, Md.



STAYLOR, 53 Charleston, S.C.



RAYMOND STAYLOR, 53 Charleston, S.C.



AVA ROBY, 54 Marysville, Ohio



GEORGE LEOHNER, 51 Chillicothe, Ohio



LINDA JANISIESKI, 42 Miamisburg, Ohio



CECILIA JANISIESKI, 71 Huber Heights, Ohio



ANONYMOUS RECIPIENT





BILL CORAM, 55 Lincolnton, N.C.



TIM SHAIN, 43 Lincolnton, N.C.



LINLEY BLENKENSOPP, 51 Patchogue, N.Y.



BLENKENSOPP, 41 Patchogue, N.Y.



KATHERINE McKINNEY, 62 Toledo, Ohio



HELEENA MCKINNEY, 29 Cincinnati Donor-in-waiting

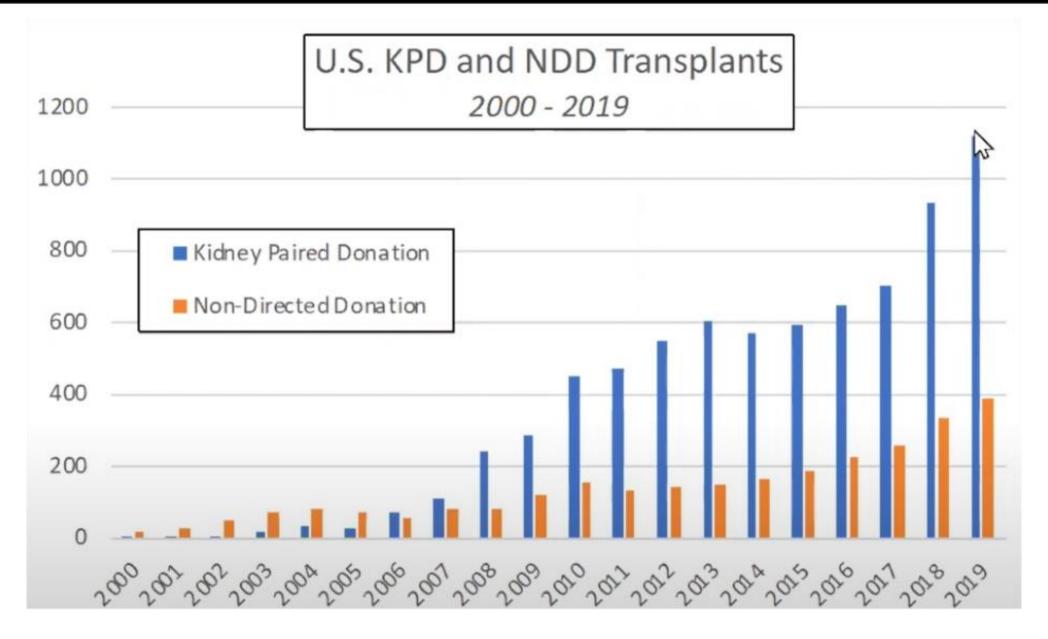


Figure source: Talk by Alvin Roth on "Kidney Exchange: An Operations Perspective" hosted by INFORMS Health Applications Society; June 2021

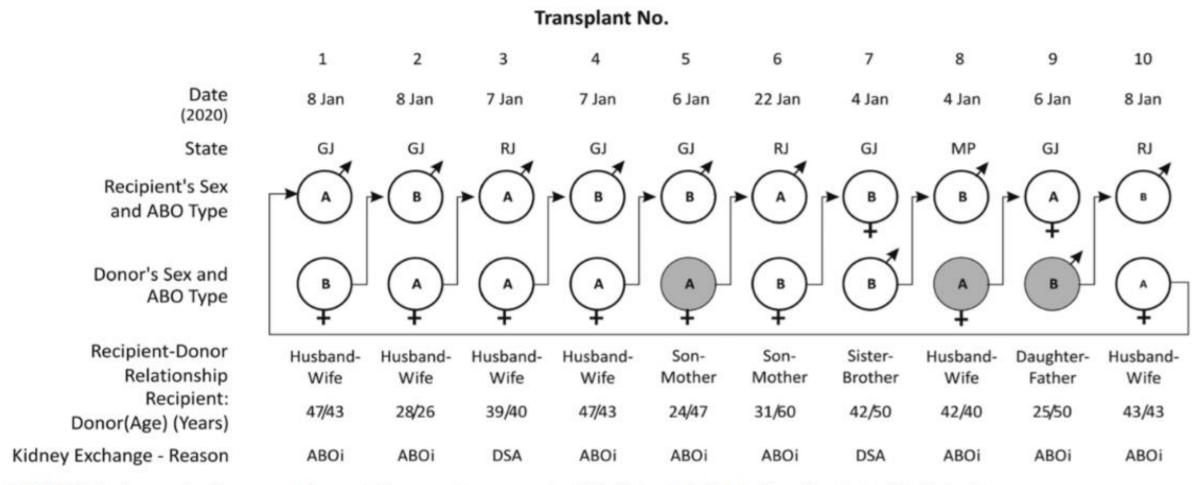


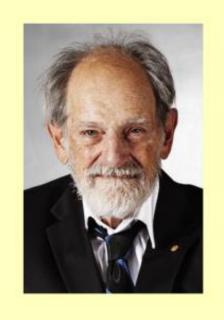
FIGURE 1. A nonsimultaneous 10-way kidney exchange cycle. GJ, Gujarat; MP, Madhya Pradesh; RJ, Rajasthan.

Kute et al. "Paired Kidney Exchange in India: Future Potential and Challenges Based on the Experience at a Single Center", Transplantation, May 2021, 105(5), pp 929-932

Sveriges Riksbank Prize in Economic Sciences in Memory of Alfred Nobel 2012



Alvin E. Roth



Lloyd S. Shapley

"for the theory of stable allocations and the practice of market design."

Challenges in Kidney Exchange

Economic: Incentives of hospitals vs maximizing overall welfare.

Computational: Finding a maximum matching using 3-cycles is NP-hard.

Informational: Patients and donors arrive sequentially.

Logistical: Long cycles require many simultaneous surgeries.

Legal: Many countries do not permit altruistic donation.

Ethical: Is it OK to buy and sell kidneys?

Next Time

Cake cutting



Housing markets and TTCA

Lloyd Shapley and Herbert Scarf "On Cores and Indivisibility" Journal of Mathematical Economics,1(1), 1974 pg 23-37 https://www.sciencedirect.com/science/article/pii/0304406874900330

Truthfulness under TTCA

Alvin E. Roth "Incentive Compatibility in a Market with Indivisible Goods" Economics Letters, 9(2), 1982, pg 127-132 https://www.sciencedirect.com/science/article/pii/0165176582900039

 The presentation is heavily inspired from Tim Roughgarden's lectures in the course on Algorithmic Game Theory (Fall 2013); see Lec 9 and 10. https://timroughgarden.org/f13/f13.html

- Data about waiting list for organs in the US: https://optn.transplant.hrsa.gov/data/
- Data about waiting list for kidneys in India (April 2019): https://www.narayanahealth.org/blog/kidney-transplants-in-india/
- Wikipedia article on "Kidney Paired Donation": https://en.wikipedia.org/wiki/Kidney_paired_donation

Proposal 1: Kidney exchange using top-trading cycles and chains

Alvin E. Roth, Tayfun Sönmez, and Utku Ünver "Kidney Exchange"
The Quarterly Journal of Economics, 119(2), 2004 pg 457-488 https://academic.oup.com/qje/article/119/2/457/1894508

Proposal 2: Kidney exchange using matchings

Alvin E. Roth, Tayfun Sönmez, and Utku Ünver "Pairwise Kidney Exchange"
Journal of Economic Theory, 125(2), 2005 pg 151-188
https://www.sciencedirect.com/science/article/pii/S0022053105001055

• The "You request my house, I get your turn" extension of TTCA was originally proposed in the context of dormitory assignment:

Atila Abdulkadiroğlu and Tayfun Sönmez "House Allocation with Existing Tenants" Journal of Economic Theory, 88(2), 1999 pg 233-260 https://www.sciencedirect.com/science/article/pii/S002205319992553X#

Altruistic donor chains:

Rees et al.

"A Non-Simultaneous, Extended, Altruistic Donor Chain" The New England Journal of Medicine, 360(11), 2009 pg 1096-1101 https://www.nejm.org/doi/full/10.1056/NEJMoa0803645

Videos, podcasts, and blogs:

https://freakonomics.com/podcast/make-me-a-match/ https://www.donordiaries.com/

https://www.youtube.com/watch?v=D3_0Bc7gbGA https://www.youtube.com/watch?v=exB1O3pTf7E https://www.youtube.com/watch?v=4NbJTcfN6UA https://www.donordiaries.com/episodes

http://marketdesigner.blogspot.com/search/label/kidney%20exchange